Titel. Patterns in biological systems --Analytical and numerical aspects of spike formation

Abstract. First a short introduction to pattern formation in Turing systems is given.

As a particular case, we consider the Gierer-Meinhardt system in the limit of small diffusivity of the activator and large diffusivity of the inhibitor. We numerically compute the time-dependent behaviour and show that very often for large times spikes are formed, even if the intermediate states vary.

Then we analytically investigate the stability of spikes and show that in a bounded domain there exists a maximum number of stable spikes. Analytical and numerical results are compared.

We outline a number of applications and current/future projects.